

# Importance of parallel scatterings

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Based on the lecture “Monte Carlo Event Generators” by Klaus WERNER, given at the summer school “Heavy Ion Collisions in the QCD phase diagram” , June 27 - July 08, 2022, Nantes, France.

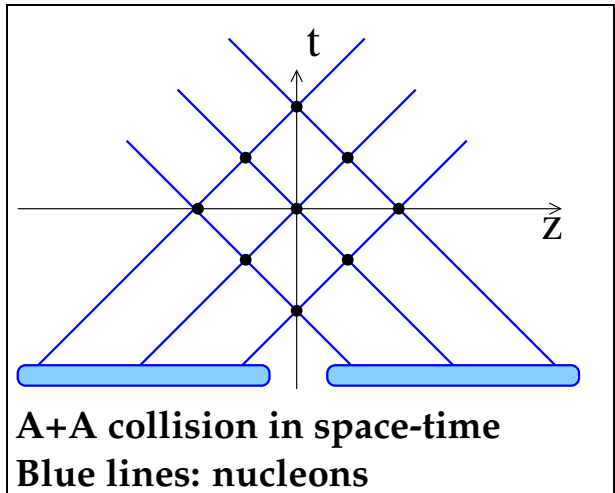
## Parallel and sequential scattering in AA

Crucial time scales

$\tau_{\text{collision}}$  is the duration  
of the AA collision

$\tau_{\text{interaction}}$  is the time  
between two NN  
interactions

$\tau_{\text{form}}$  is the particle  
formation time



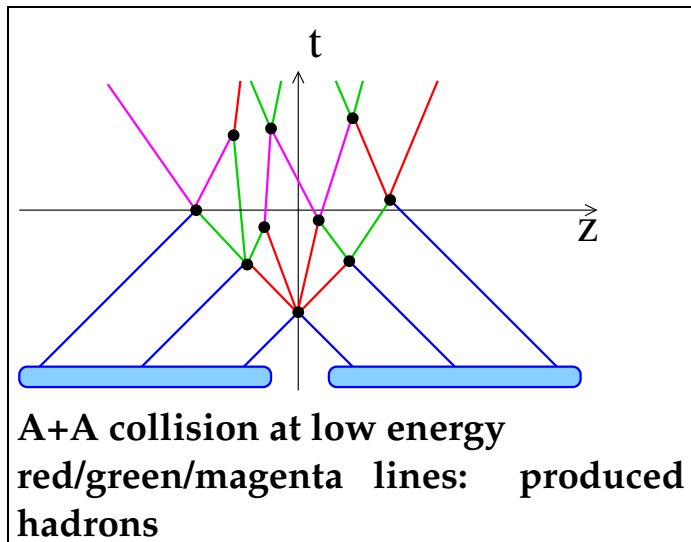
At "low" energy

Sequential  
collisions  
(cascade)

**Crucial:**

$$\tau_{\text{form}} < \tau_{\text{interaction}}$$

$\tau_{\text{form}}$  is the particle  
formation time  
 $\tau_{\text{interaction}}$  is the time  
between two NN  
interactions



At “high” energy ( $\gg 1\text{GeV}$ ):  
Longitudinal size

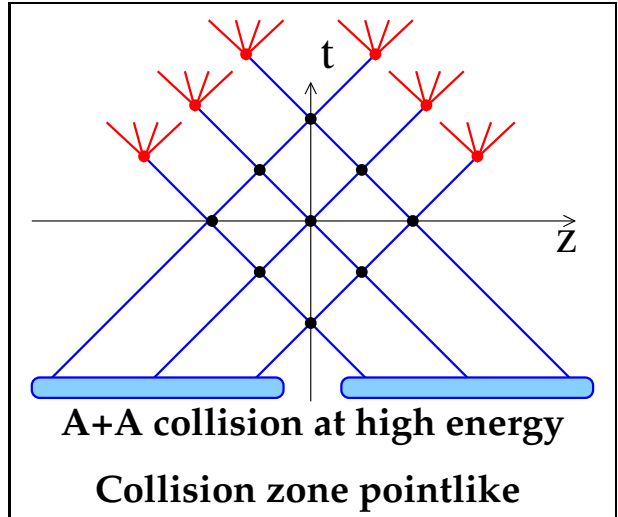
$$d = \frac{2R}{\gamma} \ll 1 \text{ fm}/c$$

All interactions  
simultaneously  
at  $t = 0$  (in parallel)

Particle production  
later. Condition:

$$\tau_{\text{form}} \gg \tau_{\text{collision}}$$

$\tau_{\text{collision}}$  is the duration  
of the AA collision



**Low energy and high energy nuclear scattering are completely different, and completely different theoretical methods are needed**

- **High energy approach = parallel interactions  
(as done in EPOS)**

(and this is why we need these Markov chain techniques...)

- **At LHC energies, one can completely separate**
  - **primary interactions (within  $< 0.01$  fm/c)**
  - **and secondary interactions (hydro evolution etc)**

What is the range of validity of the “parallel approach” ?

The condition is

$$\tau_{\text{collision}} = \frac{2R}{\gamma c} < \tau_{\text{form}} \approx 1 \text{ fm}/c$$

For  $R = 6.5 \text{ fm}$ , we get

$$\gamma > \frac{2R}{c\tau_{\text{form}}} \approx \frac{13}{1}$$

so the critical energy per nucleon is  $E \approx 13 m_p c^2 \approx 12 \text{ GeV}$

**The “parallel approach” is valid (and required) for  $\sqrt{s_{NN}} \gtrsim 24 \text{ GeV}$  (upper BES energies, LHC)**

What is the range of validity of the “cascade approach” ?

The condition is (with  $n$  nucleons in a row)

$$\tau_{\text{interaction}} = \frac{2R}{n\gamma\beta c} > \tau_{\text{form}} \approx 1 \text{ fm}/c$$

For  $R = 6.5 \text{ fm}$  and  $n = 6$ , we get

$$\gamma\beta < \frac{2R}{nc\tau_{\text{form}}} \approx \frac{13}{6}$$

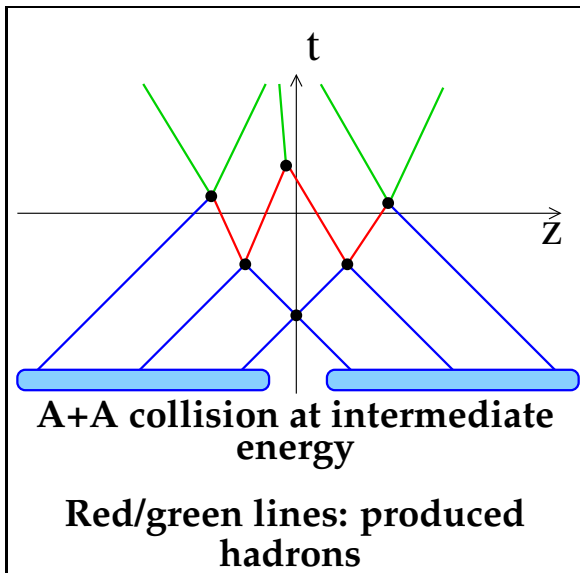
so the critical energy per nucleon is  $E \approx \gamma m_p c^2 \approx 2.2 \text{ GeV}$

**The “cascade approach” is valid for  $\sqrt{s_{NN}} \lesssim 4 \text{ GeV}$**

## The intermediate range $4 < \sqrt{s_{NN}} < 24$ GeV

On needs a  
“partially parallel  
approach”

Several (but not  
all) NN scatterings  
are realized, before  
particle production  
starts



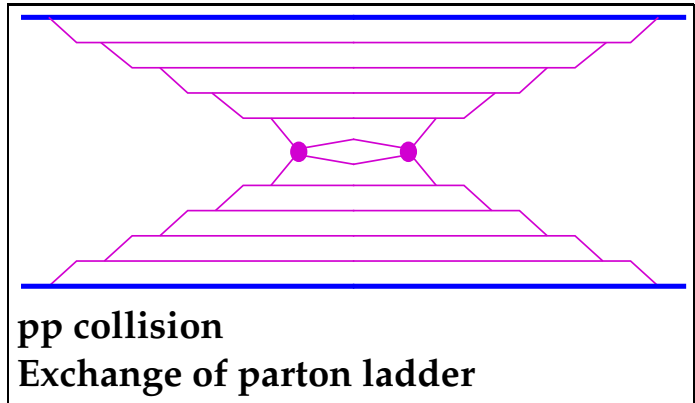


## Parallel approach in pp

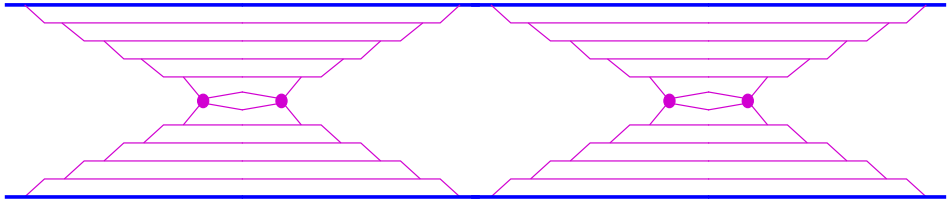
At LHC energy: Interaction: successive parton emissions

Large gamma factors, very long lived ptls

The complete process takes a very long time



Impossible to have several of these interactions in a row



So also in pp:

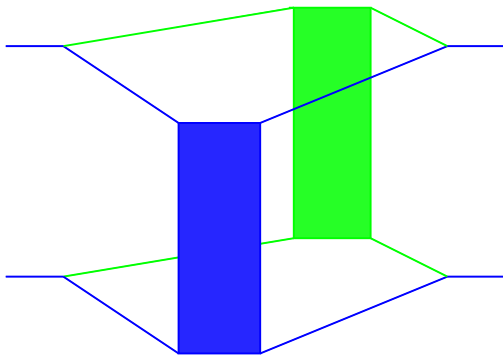
- **High energy approach = parallel interactions  
(as done in EPOS)**

**And we know that multiple scattering is important!**

So double scattering in pp should look like this:

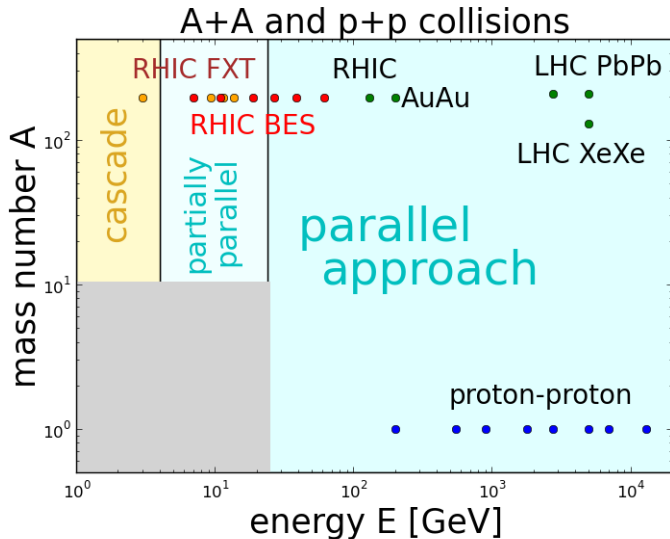
Here two parallel scatterings

No contradictions with respect to timescales



So it seems mandatory to use a parallel scattering scheme, for pp and AA, known since a long time ... but somewhat forgotten nowadays ...

## Parallel approach needed almost everywhere



Points  
(besides FXT):  
Epos  
comparisons  
to data